## 5

## Probability Models

## Calculator Note 5A: Computing Relative Frequencies From a Frequency Table

A frequency table can easily be converted into a relative frequency table using the List Editor of the TI-83 Plus or TI-84 Plus. This allows you to assign probabilities based on observed data (long-run relative frequencies). First enter the possible values into list $\mathrm{L}_{1}$ and enter the frequencies into list $\mathrm{L}_{2}$. Then define list $\mathrm{L}_{3}$ as the relative frequencies with the expression $\mathrm{L}_{2} / \mathrm{sum}\left(\mathrm{L}_{2}\right)$. Find the sum (command by pressing [2ND [LIST], arrowing over to MATH, and selecting 5:sum(.
For example, here are the data from Display 5.2 on page 290 of the student book.

| L1 | L2 | - ¢ |
| :---: | :---: | :---: |
| 0 1 2 | $\begin{aligned} & 7 日 z \\ & 1493 \\ & 725 \end{aligned}$ | $\begin{aligned} & 2607 \\ & 2967 \\ & 24167 \end{aligned}$ |
|  |  |  |

## Calculator Note 5B: Performing Many Runs of a Simulation

You can use the TI-83 Plus or TI-84 Plus to simulate flipping a coin, keep track of the cumulative proportion of heads, and make a graph similar to Display 5.4 on page 293 of the student book.
a. Enter the flip numbers into list L , for example, the whole numbers 1 to 150 . The sequence command, found by pressing [2ND [LIST], arrowing over to OPS, and selecting $5:$ seq(, is a convenient way to enter these whole numbers. Enter the command in the form seq(formula, variable, start, end, increment). For example, define list $\mathrm{L}_{1}$ with the expression $\operatorname{seq}(\mathbf{X}, \mathbf{X}, \mathbf{1}, \mathbf{1 5 0 , 1})$.

b. Enter the outcomes of the flips into list $\mathrm{L} 2: 1=$ heads or $0=$ tails. To simulate flipping a fair coin that has 0.5 probability of heads, use the random integer generator randInt $(0,1,150)$. You find the randint ( command by pressing (IATH), arrowing over to PRB, and selecting 5:randInt(. The command's syntax is randInt(lower integer, upper integer, number of trials). That is, randInt $(0,1,150)$ randomly selects 0 or 1 one hundred fifty times with equally likely results.

To simulate a coin that has a different probability of heads, for example, 0.4, use the random binomial generator randBin $(1,4,150)$. You find the randBin( command by pressing (MATH, arrowing over to PRB, and selecting 7:randBin(. The command's syntax is randBin(number of trials, probability of success, number of simulations). Because you want the individual results from 150 flips, number of trials equals 1 and number of simulations equals 150 . That is, $\operatorname{randBin}(1,4,150)$ randomly selects 0 or 1 one hundred fifty times where the probability of success ( $1=$ heads) is 0.4 . You'll learn more about binomial probability in Chapter 6 of the Statistics in Action student book, and you'll revisit the randBin( command in Calculator Note 8A.
c. Define list $\mathrm{L}_{3}$ as the cumulative number of heads, cumSum( $\mathrm{L}_{2}$ ). Find the cumSum ( command by pressing [2ND [LIST], arrowing over to OPS, and selecting 6:cumSum(.

| 5 | L2 | T | 3 |
| :---: | :---: | :---: | :---: |
| $\begin{array}{\|l} \hline \frac{1}{2} \\ 3 \\ 4 \\ 5 \\ 5 \\ \hline 6 \end{array}$ | $\begin{aligned} & 0 \\ & 0 \\ & 1 \\ & 1 \\ & i \\ & 0 \\ & i \end{aligned}$ |  |  |
| Ls =GumSum(Lz) |  |  |  |

d. Define list L 4 as the proportion of heads accumulated after each flip, or list L3 divided by list L 1 .


| L2 | L2 | L4 | 4 |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |
| 0 | 0 | 0 |  |
| 1 | 1 |  |  |
| 1 | 1 |  |  |
| ì | $\underline{2}$ |  |  |
| 1 | 3 |  |  |
| L4 $410=0$ |  |  |  |

e. Make a scatterplot of the proportion of heads accumulated after each flip ( L ) versus the number of the flip ( L ). Tracing the plot supports the Law of Large Numbers. For this simulation, as the sample size gets larger, the sample proportion approaches the population proportion of 0.5 .


$[-10,160,10,-0.2,1.2,0.1]$

$[-10,160,10,-0.2,1.2,0.1]$

## Calculator Note 5C: Using a Program to Perform Many Runs of a Simulation Involving Two Events-The WASH Program

This program will perform many runs of the simulation for the Men and Women and Hand Washing example on pages 305-306 of the Statistics in Action student book. The program can be modified for other similar scenarios.

This program is written to run the simulation 500 times, selecting one man from a population of $75 \%$ hand washers and one woman from a population of $90 \%$ hand washers and then comparing the two and recording whether the combination is both washed, man washed/woman didn't, both didn't wash, or man didn't wash/woman did. The number of each outcome is reported, in that order

Line 5 of the program can be modified for a different number of runs, and lines 6 and 7 can be modified to change the probability of a success.

| Progrimi whsh | Else |
| :---: | :---: |
| $0 \cdot \mathrm{~A}$ | $\mathrm{B}+1 \rightarrow \mathrm{~B}$ |
| -9, ${ }^{\text {B }}$ | End |
| 090 | Else |
| $0 \cdot \square$ | If $\mathrm{W}=0$ |
| For ( $1,1,506$ ) | Then |
| randBin $(1, .75)$ ¢ 11 | $\mathrm{C}+1 \rightarrow \mathrm{C}$ |
| randBinc 1 , . 9 ) 9 W | Else |
| If $\mathrm{M}=0$ | $\mathrm{D}+19 \mathrm{C}$ |
| Then | End |
| If $\mathrm{\omega}=0$ | End |
| Then | End |
| $\mathrm{F}+1 \boldsymbol{*} \mathrm{H}$ | Disf CH, B, C, D) |

